Data driven functional regions

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1 Introduction

National scale changes in social, economic, and demographic variables are the result of a diverse range of interactions at the local, regional, national, and international level. Even within a single local area, there are a myriad of factors driving change and promoting stability and/or instability (Green & Owen 1990). The past several decades have seen increasing recognition that the standard administrative areas used by governments for policy making, resource allocation, and research do not provide meaningful information on actual conditions of a particular place or region (Ball 1980, Casado-Díaz 2000). As such, there has been a move towards the identification and delineation of functional regions, commonly based on the conditions of local labour markets (Smart 1974, Casado-Díaz 2000, Coombes 2002, Watts 2004). Ball (1980) suggests that the use of a spatial definition of local labour market conditions, such as functional regions, is of particular relevance for several reasons, including as a means of presenting information and statistics on employment and socio-economic structures, as well as assessing the effectiveness of regional policy decisions, and local government reorganisation.

Journey to work behaviour is widely cited as one of the most appropriate indicators of local labour market dimensions (e.g., Ball 1980, Gerard 1958, Vance 1960, Hunter 1969), and as a result, is often used to develop functional regions. As such, a functional region is often defined as a geographical region in which a large majority of the local population seeks employment, and the majority of local employers recruit their labour (Ball 1980, Coombes & Openshaw 1982, Casado-Díaz 2000). Functional regions are generally produced via a delimitation procedure which considers the direct and indirect relationships between regions by analysing the behaviour of individual commuters (Cörvers et al. 2008).

A number of regionalisation procedures have been suggested in the litterature (e.g., Masser & Brown 1975, Slater 1981, Coombes et al. 1986, Flórez-Revuelta et al. 2008), the most successful likely being that proposed by Coombes et al. (1986). The aim of this procedure is to define as many functional regions as possible, subject to certain statistical constraints which ensure that the regions remain statistically and operationally valid (Coombes & Casado-Díaz 2005). Similar definitions of functional regions has been employed in the Netherlands (Laan 1991) and other parts of Europe (Eurostat 1992), and more recently in Spain (Casado-Díaz 2000), and New Zealand (Papps & Newell 2002).

2 Issues

One thing that becomes immediately apparent when considering the regionalisation procedure of Coombes et al. (1986) and related algorithms is the seemingly arbitrary choice of threshold values. These threshold values will largely determine the size and number of functional regions defined, and can greatly influence the results of the regionalisation exercise. Others have argued against the use of situation-dependant absolute threshold values (e.g., Cörvers et al. 2008), or have suggested alternatives, such as using relative instead of absolute values (e.g., Laan & Schalke 2001). Despite these attempts, there remains few alternative methods in the geographical literature which do not rely to some degree on arbitrary criteria, and even fewer still being used in practise.

An additional problem with many functional regionalisation procedures is that they cannot be used directly for selecting the *number* of functional regions, k. Indeed many procedures require the value of k to be specified a *priori* Brown & Holmes (e.g., 1971), Masser & Scheurwater (e.g., 1980), Baumann et al. (e.g., 1983), Cörvers et al. (e.g., 2008), or determine k through the use of ad hoc assessments of the data. For example, many researchers have relied on subjective assessments of the configuration of functional regions, often based the authors' perceptions of local environments and specific application contexts to determine the optimal number of functional regions (Noronha & Goodchild 1992). As Noronha & Goodchild (1992) point out, it is difficult to maintain confidence in assessments of validity such as "These results agree *fairly well* with the regions used by the government for planning and statistics..." (Hollingsworth 1971,emphasis added by Noronha & Goodchild (1992)), or "The functional regions produced by the approach outlined above ... conformed *extremely closely* to an *intuitive knowledge* of the study area." (Brown & Holmes 1971, emphasis added by Noronha & Goodchild (1992)).

3 Alternative

Alternatives to standard clustering methods for interaction data include a range of network-based methods which have been developed in fields as diverse as computer science, sociology, biology, and physics (White & Smyth 2005, Newman 2006a,b). Early examples include the Kernigan-Lin algorithm (Kernighan & Lin 1970), spectral clustering (e.g., Ng et al. 2002,Verma & Meila 2003, Fischer & Poland 2004), as well as several hierarchical clustering methods (e.g., Murtagh 1983). One thing that many of these methods have in common is that they are designed to find the 'community structure' of a network, which is generally defined as the underlying clustering of nodes within the network. In this sense, community structure refers to the tendency for nodes in a network to form groups of high withingroup edge connections, and low between-group edge connections (Newman 2004b). There are a range of applications for this type of cluster analysis, including finding groupings in social networks, describing the structure of communication and distribution networks, as well as finding functional regions within interaction data.

While many of the methods described above are fast, effective tools for partitioning a network dataset into relevant clusters, there are several shortcomings inherent in these methods which make them difficult to use for many applications. For example, the majority of these approaches attempt to balance the size of the detected clusters while minimising the interaction between groupings, which leads to a partitioning of the dataset into clusters of relatively equal size (Ng et al. 2002). While this may be optimal for parallel processing in computer science, many real world phenomenon do not exhibit this type of clustering, and as such, the optimal grouping in this type of data may not be found using spectral or hierarchical clustering methods. Furthermore, most spectral and hierarchical clustering algorithms are not able to provide an estimate of the number of clusters or grouping in a dataset, since they are designed to find groupings based on a predefined value of k.

Recently, a range of new clustering algorithms based on the 'modularity function' of Newman & Girvan (2004), have been developed (e.g., Newman 2004a,b, Clauset et al. 2004, Leicht & Newman 2008). These methods have in turn been further refined to take advantage of the speed of spec-

tral clustering methods, while maintaining the benefits of the 'modularity function' Q of Newman & Girvan (e.g., White & Smyth 2005, Newman 2006a,b, Leicht & Newman 2008). This Q function directly measures the quality of a particular cluster arrangement, providing a means to automatically select the optimal number of clusters (or functional regions) k, in a network by choosing the cluster arrangement where Q is maximised. This has the direct benefit of eliminating the need for arbitrary cut-off values or parameters, as well as providing a concrete justification for the number of detected functional regions or clusters. Furthermore, spectral clustering algorithms that attempt to optimise the Q function will preferentially choose cluster arrangements where "there are many edges within [clusters] and only a few between them." (Clauset et al. 2004,p.066111-1). This definition of an optimal cluster arrangement agrees closely with the aim of most functional regionalisation procedures, and as such is particularly suited to our functional regionalisation problem.

4 Origins & destinations

For the present study, travel-to-work data was obtained for the entire Republic of Ireland from the Place of Work Census of Anonymised Records (POWCAR) from the Census of Population of Ireland 2006 (CSO 2006). This dataset contains anonymised geo-coded journey to work details (origin and destination) of all employed individuals in Ireland who regularly commute, as well as a range of demographic and socio-economic characteristics, including sex, age group, marital status, education, socio-economic group, employment type, and means of travel (CSO 2006). For our analysis, the origins and destinations are geo-coded to their corresponding electoral district (ED), and from this we are able to generate a generalised network of flows between each ED. In this way, we are able to examine the effects of different scocio-economic variables by changing the weights of the network edges to reflect the movements of particular employment- and person-types, such as 'highly educated female executives'. The allows us to develop socio-economic *functional regions*, which will help to provide a perspective on socio-economic influences on the local labour market. By subjecting the above commuting network to a spectral variant of the Newman modularity cluster algorithm (e.g., White & Smyth 2005, Newman 2006b, Leicht & Newman 2008), we will be able to highlight the underlying community structure of the travel to work network, effectively generating a range of functional regions based on the interconnections of the origins and destinations in the POWCAR dataset.

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